

CHARACTERISTIC LINES (YEARLY PERMANENT LEVEL LINES) AND  
CHARACTERISTIC WIND VARIABLES FOR WIND ENERGY PRODUCTION

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CHARACTERISTIC LINES (YEARLY PERMANENT LEVEL LINES) AND  
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Hans Pigge\*

We believe that the following article will be very important /704\*\* for evaluating wind power generation for supplying electrical energy. Important variables are derived for the design power level and the yearly energy based on the yearly permanent level lines. The article gives us an idea of what is contained in the wind (the publishers).

B. Koetzold, Director of the electrical plant, Wesertal GmbH, Hameln, has considered the international importance of wind power production for the electrical economy. He has suggested \*\*\* that characteristics for the wind be prepared in the form of yearly permanent level lines. This is to be done for the specific raw wind power ( $\text{kW/m}^2$ ) and for the specific yearly raw wind energy

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\* Hameln. Lecture held at the Wind Generation Meeting at Oldenburg 1.0. on May 13, 1955.

\*\* Numbers in the margin indicate pagination of original foreign text.

\*\*\* Discussion of the lectures by K. Schneider-Carius, meteorological considerations for exploiting air flows for the purpose of wind power production and W. Caspar, evaluation of the wind data for wind power generation in Germany, Communication No. 4 of the Wind Generation Study Group, Stuttgart, 1955. Other publications of the study association are given on Page II of this issue.

(in kWh/m<sup>2</sup>). These so-called permanent level lines are derived from the wind velocity permanent level lines [1] of a windy location and are especially important for optimum performance design. This is closely related with the available net yearly energy and the economy of the installation, i.e., the net costs per kilowatt hour. Similar calculations are performed for hydroelectric power.

The author has taken up this suggestion, i.e., the mentioned permanent level lines have been drawn for three characteristic wind locations (measurement stations of the German Weather Service) based on the "Wind Data" \*. This refers only to the raw values for wind power and yearly wind energy which is contained in the wind and which refers to one m<sup>2</sup> of area  $F_R$ . The absolute magnitudes can be obtained from the specific raw values by multiplying them with the wheel area  $F_R$  (m<sup>2</sup>), the working characteristic variables (power coefficient  $C_1$  and total efficiency  $\eta$ ) and the exploitation degree  $\Sigma p$ , to be defined later on.

A number of basic relationships were discovered when these permanent level lines were established. These give a relatively simple overview of wind conditions which is why we would like to discuss them here.

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\* Data for distribution of wind velocity in Germany for wind power generation, written by the Climate Division of the German Weather Service, Bad Kissingen, at the request of the Wind Power Generation Study Group, e. V., Stuttgart. Author W. Caspar, Communication No. 3 of the Wind Generation Study Group, Stuttgart, 1954.

## I. CHARACTERISTICS (YEARLY PERMANENT LEVEL LINES)

The investigation was restricted to three measurement stations, which are examples for low, medium and high average wind velocity  $V_m$ :

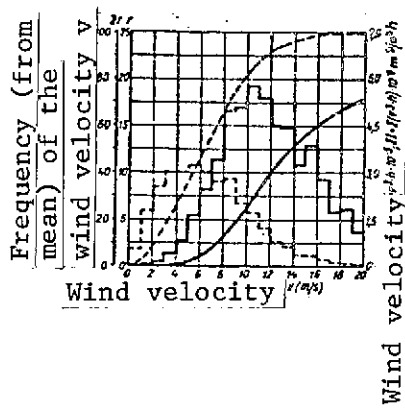
Altenwalde-Cuxhaven	$v_m = 4,37 \text{ m/s,}$
Helgoland	$v_m = 6,66 \text{ m/s,}$
Brocken	$v_m = 10,12 \text{ m/s.}$

Figure 1 shows the characteristic drawing for the Helgoland Station in the representation of "wind data". The dashed, step line is the average wind frequency (wind velocity) over a year, i.e., the percentage of hours over the year which the wind velocity indicated on the abscissa occurs (intervals of 1 m/s). The dashed curve is the sum curve of the frequency distribution. If we also form the arithmetic mean of the third power of the interval velocity from  $v_n$  to  $v_{n+1}$ , corresponding to the dependence of the wind power or the wind energy on the third power of wind velocity  $v$ , that is

$$\bar{v}^3 = \frac{v_n^3 + v_{n+1}^3}{2} \quad (1)$$

and if we multiply with the absolute magnitude of the corresponding yearly hours, then we obtain a numerical value  $J$  proportional to the wind energy of the  $v$  intervals having the dimension  $\text{m}^3\text{s}^{-3}\text{h}$ . These magnitudes  $J$  are shown by the solid step curves as a function of wind velocity. The solid curve gives the sum curve of the energy intervals. The final value of the energy sum curve represents the yearly raw power energy  $\Sigma J$  of the wind location. It is as follows for the three stations:

Altenwalde-Cuxhaven	$2,1 \cdot 10^6 \text{ m}^3\text{s}^{-3}\text{h} \text{ (} v = 0 - 20 \text{ m/s)}$
Helgoland	$5,5 \cdot 10^6 \text{ m}^3\text{s}^{-3}\text{h} \text{ (} v = 0 - 25 \text{ m/s)}$
Brocken	$16,8 \cdot 10^6 \text{ m}^3\text{s}^{-3}\text{h} \text{ (} v = 0 - 35 \text{ m/s)}$



Station altitude  
above sea level 56 m,  
transducer 21 m over  
the ground, time period  
1935/1936 and 1939.

Figure 1. Example for wind evaluations according to the "wind data" (Helgoland Station)

This representation has the advantage that from it the energy magnitudes corresponding to the individual  $v$  intervals can be read off directly or by forming differences. In addition, all variables can be represented over the entire  $v$  range with about the same absolute accuracy. However, often it is desired to have a direct relationship between time and the corresponding power and energy input, which makes it necessary to make a calculation involving the wind velocity. In addition, for energy purposes, it is also of interest to know the power and energy magnitudes on a kW or kWh scale contained in the wind, which is why it is important to draw the so-called permanent level lines. It seems appropriate to first define the permanent level line. According to the "concept definitions for energy industry" [2], a "permanent level line is a conversion of a variation line with respect to magnitude over a time interval.<sup>[1]</sup>" The variation line represents the variation of the variable over time. The permanent level line can be used to determine how long the maximum value of the variable occurs as well as its components over the time interval under discussion. Figure 2 shows an

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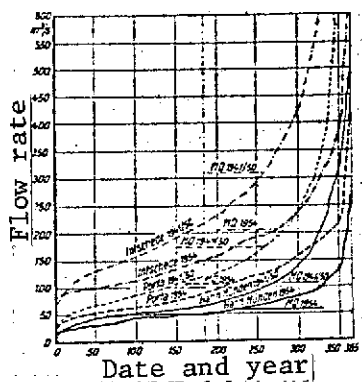


Figure 2. Official representation of the flow rate lines (Weser flow region, 1954)

official representation by the water and shipping administration. The time axis is divided into days. Because of the small daily fluctuation of the rivers, this results in a sufficient accuracy. We would like to mention that this is not the representation of the permanent level line usually given in the electrical industry. Usually the maximum values are on the left, but here the maximum values are on the right. The difference is not

important. In the electrical industry, when for example the maximum load or the heat consumption of a steam generation plant is represented, usually we are interested in limited maximum values (capacity). In the water power generation industry (also in the wind power generation industry), the maximum values are statistical average values and their values cannot be determined uniquely .

Figure 3 shows the yearly permanent level lines of the wind for the measurement station Helgoland. The following are plotted on a relative and absolute scale (hours) along the time axis:

1. The wind velocity  $v$  (in intervals of  $n = 1$  m/sec).
2. The specific raw wind power  $L_0$  (in  $\text{kW/m}^2$ ), calculated

according to the relationship

$$L_0 = 6.14 \cdot 10^{-4} v^3 \text{ (kW/m}^2\text{)} \quad *$$
(2)

where  $v^3$  is the arithmetic mean according to Equation (1), in accordance with the "Data".

3. The specific raw energy  $W_0$  (in kWh/m<sup>2</sup>) of each  $v$  interval and to  $n + 1$ .
4. The specific yearly raw wind energy  $\Sigma W_0$  (in kWh/m<sup>2</sup>) (from the sum of  $W_0$  values). This energy sum  $\Sigma W_0$  therefore represents approximately the area under the  $L_0$  curve, that is

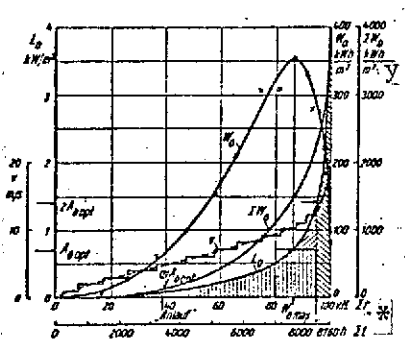
$$\Sigma W_0 = \int_0^{\infty} L_0(v) dt(v) \text{ (in kWh/m}^2\text{)} \quad (3)$$

if  $dt$  is the time interval in hours corresponding to each  $v$  interval  $n$  to  $n + 1$ .

These four permanent level lines give an accurate description of the wind variation at a windy location. All the parameters derived from the wind velocity  $v$  were reduced to unit area swept out by the wind, in order to obtain universal variables. This was already mentioned.

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\* This relationship is obtained for the performance formula for a wind wheel  $L = \frac{F_R \cdot v^3 \cdot c_1}{2 \cdot 102} \text{ (kW)}$  with a power coefficient  $c_1 = 1$  air density of  $\rho = 1.225$  for 15° C and a wheel area of  $F_R = 1 \text{ m}^2$ . The power  $L_0$  is the raw power level for 1 m<sup>2</sup> of wind passage area.



Measurement height above nominal sea level  $H_N = 77$  m, measurement above ground  $H_G = 21$  m

$$\left[ v_m = 6.66 \text{ m/s}, A_{0 \text{ opt}} = 0.70 \text{ kW/m}^2 \text{ at } v_H = 10.4 \text{ m/s}, \Sigma W_0 = 3340 \text{ kWh/m}^2, \right. \\ \left. \Sigma P_{\text{max}} = 56.2 \text{ v. H.}, \Sigma T_{\text{max}} = 56.3 \text{ v. H.} \right]$$

Figure 3. Yearly duration lines of the wind for average wind velocity  $v_m$  (Helgoland)

Translator's note: Illegible in foreign text.

This design power level produces the maximum amount of energy for the corresponding  $v$  interval. Figure 3 shows the optimum design power level  $A_{0 \text{ opt}}$ , which is calculated according to the following relationship:

$$L_{\text{ob}} = A_{0 \text{ opt}} = \frac{W_{0 \text{ max}}}{dt(v_{W_{0 \text{ max}}})} \text{ (kW/m}^2\text{)} \quad (4)$$

The following numerical values for  $A_{0 \text{ opt}}$  are obtained for the three stations mentioned above:

Altenwalde-Cuxhaven	0.377 kW/m <sup>2</sup>
Helgoland	0.70 kW/m <sup>2</sup>
Brocken	2.30 kW/m <sup>2</sup>

The yearly raw energies  $\Sigma W_0$  are:

The variation of the characteristic variables shows that only the  $W_0$  curve has a maximum. This is a natural law which can be formulated as follows: in any time-dependent frequency distribution of a statistical variable with uniform intervals, there is a region which contains the maximum value of the time function of the static variable (energy). It is natural to establish a correspondence between this energy maximum and the so-called design power level when wind power generation is discussed.



Altenwalde-Cuxhaven	1285 kW/m <sup>2</sup> ·   y.
Helgoland	3390 kW/m <sup>2</sup> ·   y.
Brocken	10 600 kW/m <sup>2</sup> ·   y.

If it is also assumed that a wind generation station starts to deliver power at a raw power level of one tenth of the optimum design power level, that is at

$$L_{of} = 0.1 A_{o \text{ opt}} \text{ (kW/m}^2\text{)} \quad (4a)$$

the area segment between these limiting values  $L_{of}$  and  $L_{ob}$  under the  $L_o$  curve represents the specific raw wind energy which can be exploited by a wind generation station. This area is shown by vertical shading in Figure 3. It can also be seen that part of the raw wind power can be used which is greater than  $A_{o \text{ opt}}$ . In the figure it is assumed that the installation can remain in operation up to twice the power level, that is for

$$L_{os} = 2 A_{o \text{ opt}} \text{ (kW/m}^2\text{)} \quad (4b)$$

but there is a downward adjustment of the design power level  $A_{o \text{ opt}}$ . This part is also shown with vertical lines shading. The entire area with vertical shading below the  $L_o$  curve is the maximum exploitable raw wind energy under the conditions mentioned above.

The area with diagonal shading are energy segments which cannot be exploited. We do not have to mention the fact that in /706 practice, the power levels or energies calculated in this way cannot be obtained. This is because the performance coefficient  $c_1$  and the total efficiency  $\eta$  are smaller than one and, in addition, the public network requires that the generating plant is usually operated at a constant rotation rate. An installation controlled by the wind variations and subjected to constant rotation

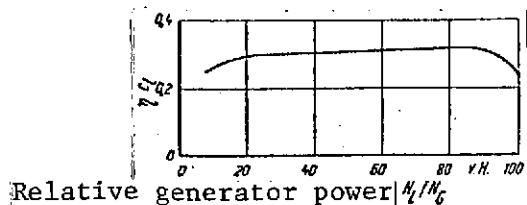


Figure 4. Dependence of  $\eta_{c1}$  on the relative generator power output for the 10 m Allgaier installation, Type D 8

characteristics are not shown in Figure 3. This is best represented if the variation of  $\eta_{c1}$  of a wind generation station is known as a function of the percentage power level  $N_L$ , that is, the power level divided by the design power level of the generator  $N_G$ . Figure 4 shows this for the 10 m Allgaier installation.

It is appropriate to divide the permanent level lines into the following five regions:

1. The zero wind region.

$$v = 0 \text{ to } v_f \quad (m = 0 \text{ to } 0.1) \quad * \quad \text{not exploitable}$$

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\*  $m$  is the factor which must multiply  $A_{opt}$  in order to obtain the power  $L_0$  for the corresponding region according to the assumptions above, i.e.,  $m = L_0/A_{opt}$ .

rate results in additional losses. The purpose of the permanent level lines is only to show the method of analysis. The performance and energy characteristics for a specific wind generation station are obtained by considering the  $\eta$ - and the  $c_1$  values and their variations as a function of wind velocity. These characteristics would run somewhat below the  $L_0$  or  $W_0$  characteristics, respectively. For clarity, these

2. The operational range proper  
 $v = v_f \text{ to } v_b$       ( $m = 0.1 \text{ to } 1$ )      exploitable
3. The operational range with control\*  
 $v = v_b \text{ to } v_s$       ( $m = 1 \text{ to } 2$ )      exploitable
4. The path control region \*  
 $v = v_b \text{ to } v_s$       ( $m = 1 \text{ to } 2$ )      not exploitable
5. The storm condition region  
 $v = v_s \text{ to } \infty$       ( $m = 2 \text{ to } \infty$ )      not exploitable

## II. CHARACTERISTIC VARIABLES

1. Optimum Raw Design Power Level  $A_{O \text{ opt}}$  and Maximum Raw  
Energy Exploitation Efficiency  $\Sigma p_{\max}$

By dividing the permanent level lines into five regions, we obtain a few additional directives for the theoretical treatment of the wind variation. It is necessary to investigate a few characteristic variables and their variations. We have already become familiar with one of the variables, the specific raw design power level  $A_{O \text{ opt}}$ . A second variable is called the maximum raw energy exploitation efficiency  $\Sigma p_{\max}$  and is defined as the ratio of the exploitable fractions (2. + 3.) in the five regions and the total raw wind energy.

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\* The technical literature contains the term "sail condition" for this range, with the exploitable fraction (3) and the loss fraction (4).

The absolute and relative magnitudes of the energy contributions in the five regions mentioned above are the following:

1. "No wind"

$$(m = 0 \text{ to } 0.1) \quad \Sigma W_{of} = \int_0^{v_f} L_o(v) dt(v) \quad p_f = \frac{\Sigma W_{of}}{\Sigma W_o} \quad (5a)$$

2. "Operation"

$$(m = 0.1 \text{ to } 1) \quad \Sigma W_{ob} = \int_{v_f}^{v_b} L_o(v) dt(v) \quad p_b = \frac{\Sigma W_{ob}}{\Sigma W_o} \quad (5b)$$

3. "Operation with control"

$$(m = 1 \text{ to } 2) \quad \Sigma W_{obr} = A_{o \text{ opt}} \Sigma t(v) \Big|_{v_b}^{v_s} \quad p_{br} = \frac{\Sigma W_{obr}}{\Sigma W_o} \quad (5c)$$

4. "Path control"

$$(m = 1 \text{ to } 2) \quad \Sigma W_{ovr} = \int_{v_b}^{v_s} L_o(v) dt(v) - \Sigma W_{obr} \quad p_{ovr} = \frac{\Sigma W_{ovr}}{\Sigma W_o} \quad (5d)$$

5. "Storm conditions"

$$(m = 2 \text{ to } \infty) \quad \Sigma W_{os} = \int_{v_s}^{\infty} L_o(v) dt(v) \quad p_s = \frac{\Sigma W_{os}}{\Sigma W_o} \quad (5e)$$

The notation in the formulas given above is found from the definitions. The limiting wind velocities  $v_f$ ,  $v_b$ ,  $v_s$  are found from the magnitudes  $L_o = m A_{o \text{ opt}}$  according to the permanent level lines.

The energy contributions according to Figure 3 can be determined from the differences of the ordinate segments of the  $\Sigma W_o$  curve (corresponding to the  $L_o$  values). The maximum raw energy exploitation efficiency is obtained as follows from the definition

$$\Sigma p_{\max} = \frac{\Sigma W_{ob} + \Sigma W_{obr}}{\Sigma W_o} = \frac{\Sigma W_{os}}{\Sigma W_{os} + \Sigma W_{on}}$$

where  $\Sigma W_{os} = \Sigma W_{ob} + \Sigma W_{obr}$  is the sum of the exploitable energy components (2. + 3.) and  $\Sigma W_{on} = \Sigma W_{of} + [\Sigma W_{ovr} + \Sigma W_{os}]$  is equal to the sum of

the nonexploitable energy fractions (1. + 4. + 5.).

The numerical Table 1 shows the percentage energy contributions  $p$  for the three measurement stations with the above assumptions, for  $m = 0.1, 1$  and  $2$ , respectively. We find that each  $p$  contribution is about as large for the three stations, and therefore independent of  $v_m$ . The zero wind contributions  $p_f$  amount to between 3 to 5% of the total yearly energy. The operational contributions are about 40-50%, the operational contributions with control  $p_{br}$  are about 15%. The remainder of the nonexploitable energy contributions consist of  $p_{wr}$  or 8%, which corresponds to the "path control" and the contribution for the "storm conditions", with a considerable contribution  $p_s$  of about 30%. The maximum raw energy exploitation efficiency is therefore obtained as  $\Sigma p_{max} =$  barely 60%  $\approx \Sigma p_{max}$ .

The contributions for the "path control" and for the "no wind conditions" are relatively small. This is why it does not make much sense to expand the assumed limits for  $m$  further upwards or downwards. It must only be determined whether it is technically possible to increase the design power level further above  $A_{o\ opt}$ , that is, further into the storm region, so that the considerable energy contribution could be exploited. For the Brocken area, the optimum design power level of  $2.3\text{ kW/m}^2$ , corresponding to a wind velocity  $v_s =$  about 20 m/sec, is probably already above the technical limits at this time, which are about 10 m/sec at this time.\*

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\* In practice, the raw design power levels of existing installations are considerably lower. For example, for the 10-m Allgaier installation,

$$A_{o\ opt} = \frac{N_g}{F_R \cdot \eta \cdot \eta} = \frac{8.8}{16.5 \cdot 0.3} = 7.5\text{ kW/m}^2 \quad \text{at } v_s = 8\text{ m/sec}$$

and  $v_f = 3\text{ m/sec}$ . This installation is optimum for the station Altenwalde-Cuxhaven.

TABLE 1. WIND VARIABLES FOR MEASUREMENT STATIONS  
ALTENWALDE-CUXHAVEN, HELGOLAND AND BROCKEN (ONLY  
VALID FOR  $m_1 = 0.1$ ,  $m_D = 1$ ,  $m_S = 2$ ) \*

Variable	Symbol Unit	Altenwalde-Cuxhaven	Helgoland	Brocken
Height above nominal sea level	$N_N$ m	34	77	1164
Height above ground	$H_G$ m	19	21	28
Height above perturbation level	$H_{GT}$ m	4	10	28
Average wind velocity	$v_m$ m/s	4.37	6.66	10.12
Optimum raw power	$A_{o opt}$ kW/m <sup>2</sup>	0.33	0.71	2.3
Yearly raw energy	$\Sigma W_o$ kWh/m <sup>2</sup>	1285	3390	10600
1. "No wind" ( $m = 0 - 0.1$ )	$v = 0$ $v_f$ m/s $P_f$ % $r_f$ %	0—4.0 3 47.0	0—4.9 3.8 40.5	0—7.2 3.2 39.5
2. "Operation" ( $m = 0.1 - 1$ )	$v = v_f$ $v_b$ m/s $P_b$ % $r_b$ %	4.0—8.5 43.6 45.4	4.9—10.5 40.8 46.7	7.2—15.5 42.7 51.5
3. "Operation with control" ( $m = 1 - 2$ )	$v_{br} = v_b$ $v_s$ m/s $P_{br}$ % $r_{br}$ %	8.5—10.6 12.3 5.0	10.5—13.3 15.3 8.3	15.5—19.5 17.1 9.0
4. "Path control" ( $m = 1 - 2$ )	$v_{br} = v_b$ $v_s$ m/s $P_{br}$ % $r_{br}$ %	8.5—10.6 7.6 5.0	10.5—13.3 8.3 8.3	15.5—19.5 8.3 9.0
5. "Storm" ( $m = 2 - 5$ )	$v = v_s$ $v_s$ m/s $P_s$ % $r_s$ %	10.6— $\infty$ 25.5 2.5	13.3— $\infty$ 31.7 4.5	19.5— $\infty$ 28.7 4.5
2. and 3. "Operation" and "Operation with control" ( $m = 0.1 - 2$ )	$v = v_b$ $v_s$ m/s $\Sigma P_{max}$ % $r_{max}$ %	4.0—10.6 61.5 55.0	4.9—13.3 56.1 60.5	7.2—19.5 59.0 60.5

\*  $m = L_o/A_{o opt}$ ,  $v_f$  Turn on wind velocity (start-up).

$v_b$  - Operation velocity (at  $A_{o opt}$ )

$v_s$  - Turn-off velocity (storm)

$r$  - Percentage of yearly hours.

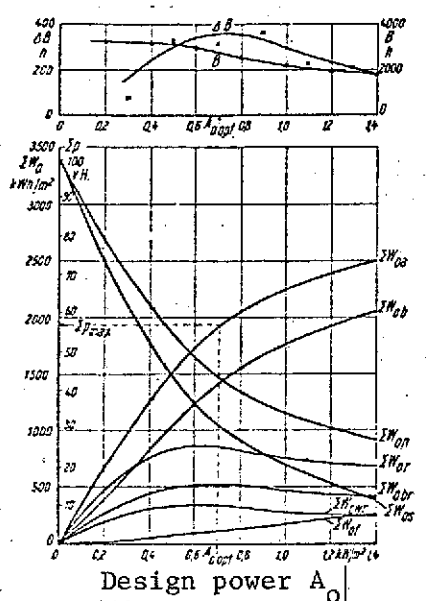


Figure 5. Variation of the energy contributions to  $\Sigma W_o$  according to Equations (5a) to (5e) for Helgoland ( $m = 0.1$ ,  $m = 1$  and  $m = 2$ )

Figure 5 (page 708) shows the variation of the energy contributions in the five regions on an absolute and relative scale for the measurement station Helgoland as a function of the design variable  $A_o$  and for the assumption  $m = 0.1$ ,  $m = 1$  and  $m = 2$ . This was done in order to determine whether the defined optimum design level is indeed an optimum for the exploitable energy. The figure was produced by measuring the area under the  $L_o$  curve for the individual regions and for the individual partial surfaces, and for various design variables  $A_o$ . This was done using a planimeter or by using the  $\Sigma W_o$  curves determined from the yearly permanent level lines plotted in a logarithmic representation and not given here. It can be seen that the contributions  $\Sigma W_{obr}$  and  $\Sigma W_{owr}$  for "operation with control" and "path control", and therefore their sum, have a well defined maximum in the vicinity of  $A_o = A_{o\ opt}$ , the contributions are small on an absolute scale, which is why these maxima are not shown in the sum curves for  $\Sigma W_{oa}$  and  $\Sigma W_{on}$ , respectively.

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The raw energy exploitation efficiency  $\Sigma p$  can be obtained from a curve for  $\Sigma W_{oa}$  for each magnitude  $A_o$ .

The upper part of Figure 5 shows the duration of use B (in hours per year)  $= \Sigma W_{oa}/A_o$  and its increment  $\Delta B$  between the indicated measurement points of  $A_o$ . It is found that the increase  $\Delta B$  does indeed have a maximum in the vicinity of  $A_o \text{ opt}$ , i.e., the function  $d\Delta B/dA_o$  for  $A_o \sim A_o \text{ opt}$ . This is a point at which there is a relative minimum of  $A_o$  and also a relative maximum of the duration of use B, as a function of the unit power level  $A_o$ . Therefore there is also a maximum in the raw energy exploitation efficiency  $\Sigma p$ , and in the exploitable yearly raw energy  $\Sigma W_{oa}$ .  $A_o \text{ opt}$  is therefore the true optimum design variable, given the assumptions for m made above ( $m_f = 0.1$ ,  $m_b = 1$ ,  $m_s = 2$ ).

Figure 6 shows the raw energy exploitation efficiency  $\Sigma p$  as a function of the power  $A_o$  referred to  $A_o \text{ opt}$ , i.e.  $\Sigma p = f(m_o) = f(A_o/A_o \text{ opt})$  for the values from Figure 5 (Helgoland) and the corresponding values for Altenwalde-Cuxhaven and the Broken region and for the assumed conditions ( $m_f = 0.1$ ,  $m_b = 1$ ,  $m_s = 2$ ). For example for the 10-m Allgaier installation built in Helgoland we obtain a raw energy exploitation efficiency of about 42% with  $m_o = 0.45/0.70 = 0.64$ .

## 2. Theoretical Raw Design Power Level $A_{oth}$ and Theoretical Yearly Raw Energy $\Sigma W_{oth}$ as a Function of $v_m$ .

It is known that there is a close relationship between the average wind velocity  $v_m$  and the raw wind power or the yearly raw wind energy level. It is natural to investigate this relationship. For this purpose, for 14 measurement stations contained in the "Data", those having the largest yearly raw wind energy, we calculated the quantities  $A_o \text{ opt}$  and  $\Sigma W_o$  mentioned above. Numerical Table 2 contains the results. Figure 7 shows this in a



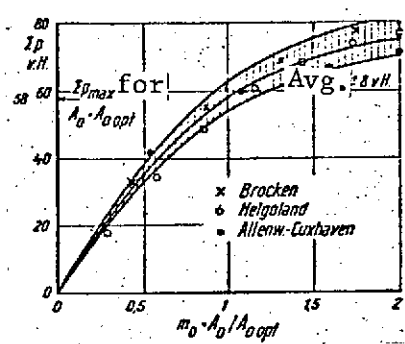


Figure 6. Dependence of the raw power efficiency  $\Sigma p$  compared with relative degree of construction

$$m_o = A_o / A_o \text{ opt}$$

graphical representation. The calculation is done according to the formulas given. It is found that, except for a large scatter in the measurement points shown with respect to the theoretical variation, there is a unique relationship between the average wind velocity  $v_m$  and the theoretical optimum specific raw design power level  $A_{oth}$ , that is the theoretical specific yearly raw wind energy  $\Sigma W_{oth}$  (only valid for  $m = 0.1$ ,  $m = 1$  and  $m = 2$ , according to the assumptions made above):

$$\begin{aligned} A_{oth} &= 3.3 \cdot 10^{-3} v_m^3 \text{ (kW/m}^2\text{)} \pm 35 \text{ v.H.} \\ \Sigma W_{oth} &= 11.6 \cdot v_m^3 \text{ (kW/m}^2 \cdot \text{y.)} \pm 14 \text{ v.H.} \end{aligned}$$

There is no dependence on the average wind velocity  $v_m$  for the maximum raw energy efficiency  $\Sigma p_{max}$  defined above, as was already found in numerical Table 1 and Figure 6. In general, with the assumptions made above ( $m = 0.1$ ,  $m = 1$  and  $m = 2$ ) an optimum value of  $\Sigma p_{max} \sim 60\%$  can be used [1]. In other words, in the best case about 60% of the yearly raw wind energy can be used. It is necessary to consider the fact that this value only applies if the short time fluctuations in the wind can be measured by the wind measuring devices by a "rapid response device".

TABLE 2. WIND VARIABLES FOR THE 14 FAVORABLE WIND STATIONS OF THE "DATA" (MAXIMUM YEARLY RAW ENERGY  $\Sigma W_0$ )

Measurement station	$V_m$	$L_{0th}$	$A_{0opt}$	$\Sigma W_0$	$\Sigma p_{max}$	$\Sigma r_{max}$	$\alpha$	$\gamma$	$v_b$	$v_b/v_m$
1. Hamburg-Fuhlsbüttel	4,39	0,0520	0,155	1060	72,0	48,0	8,74	20200	9,05	2,06
2. Altona-Cosshaven	4,37	0,0513	0,177	1285	64,8	52,5	7,35	25050	8,50	1,95
3. Bremen-Freib.	5,34	0,0911	0,264	1455	53,4	72,0	2,90	19550	7,55	1,42
4. Nauen 31 m	5,46	0,0999	0,265	1590	50,8	70,0	2,65	15930	7,55	1,38
5. Brunsbüttelkoug	5,08	0,0804	0,350	1680	63,7	48,5	4,35	20900	8,30	1,64
6. Hohenpeissenberg	4,26	0,0704	0,685	1840	48,2	36,0	9,73	26700	10,60	2,18
7. Wyk a. Fohe	6,21	0,147	0,722	2770	61,1	56,0	5,12	18250	10,70	1,73
8. Quickborn 70 m	6,72	0,186	0,736	2610	53,7	76,5	3,97	14000	10,65	1,59
9. Wasserkuppe	5,95	0,131	0,945	2550	64,1	42,0	7,23	19500	11,53	1,93
10. Helgoland	6,66	0,181	0,713	3390	55,5	60,0	3,94	18750	10,51	1,58
11. Kahler Asten	7,17	0,226	0,934	3400	83,3	70,0	4,13	15050	11,49	1,60
12. Kalmat	7,08	0,217	0,934	3950	57,9	61,0	4,30	18220	11,49	1,63
13. Feldberg	8,11	0,333	2,245	6650	62,1	48,0	6,75	20000	15,41	1,90
14. Brücken	10,12	0,635	2,370	10600	58,7	62,5	3,74	16720	15,70	1,55
Avg. values					60,7	57,8	5,35	18980		1,73

$$L_{0th} = 6,14 \cdot 10^{-4} \cdot v_m^3 \text{ kW/m}^2, \quad \alpha = \frac{A_{0opt}}{L_{0th}}, \quad \gamma = \frac{\Sigma W_0}{E_{0th}}$$

$$v_b = \sqrt{\frac{A_{0opt}}{6,14 \cdot 10^{-4}}}$$

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Since this cannot be done perfectly in practice, we could only hope to use a value of  $\Sigma p_{max} \approx 0,50$ .

Simple practical relationships are obtained with these values, so that the net characteristic variables of a specific wind generation station can easily be determined if the magnitude of the average wind velocity  $v_m$  is known for an erection site. For example, for a wind controlled installation, i.e., pitch rate  $\lambda = u/v = \text{const}$ ), the optimum net design power level is  $N = \{\eta \cdot c_1 \cdot A_{0th} \cdot F_R\} \text{ (kW)}$  and the maximum net yearly energy is  $E = \eta \cdot c_1 \cdot \Sigma p_{max} / \Sigma W_{0th} \cdot F_R \text{ (kWh)}$ .

For a net-controlled installation (rotation rate  $n = \text{const}$ ), these variables must be multiplied by the following working factor  $\eta_n \approx 0,8$  to 0.9, which is the result of the constant rotation rate [1].

For completeness, Figure 8 also shows the magnitudes of the wind velocities of the individual regions  $v_f$ ,  $v_b$ ,  $v_s$  mentioned in

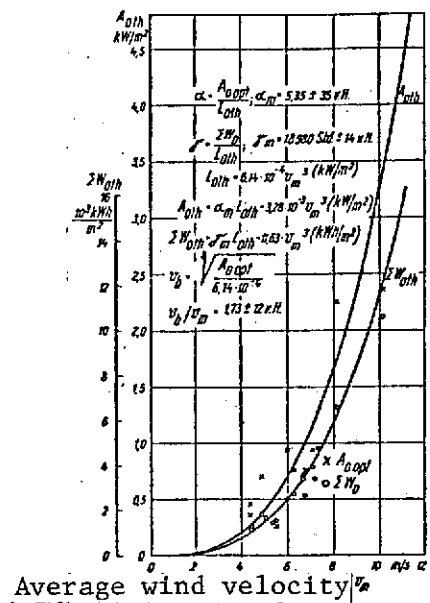


Figure 7. Dependence of the theoretical optimum raw design power  $A_{0\ th}$  and the theoretical raw yearly energy  $\Sigma W_{0\ th}$  on the wind velocity  $v_m$  according to the numerical Table 2.

$v_f$  - zero wind starting wind velocity,  $v_b$  - wind velocity for full design operational power,  $v_s$  - wind velocity for storm conditions (shut-down)

Equations (5a) to (5e) as a function of  $v_m$  assuming that  $m = 0.1$ ,  $m = 1$  and  $m = 2$ . It was calculated from the values in Table 2 for the 14 measurement stations. The theoretical linear functions are obtained as follows:

$$\left. \begin{aligned} v_{fth} &= 0.78 v_m \pm 11 \% \\ v_{bth} &= 1.68 v_m \pm 11 \% \\ v_{sth} &= 2.12 v_m \pm 11 \% \end{aligned} \right\} \text{ and}$$

## SUMMARY

This report attempts to show how the unique picture of the raw energy contained to the wind can be obtained using the yearly permanent level lines. Also the power levels and their variations can be obtained. Using graphical procedures and

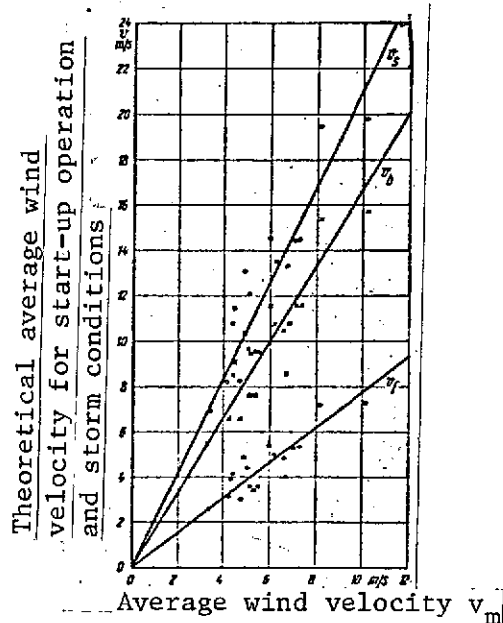


Figure 8. Dependence of the theoretical average wind velocity for start-up operation and storm conditions on the wind velocity  $v_m$

numerical tables, the raw energy contained in the wind can be obtained for optimum exploitation conditions so that each wind generation station is matched to the erection site (wind location) by proper selection of the design level (generator size). In this investigation we wanted to demonstrate the method which follows after the yearly permanent level lines have been established. It would be desirable if wind generation plant designers would use this data to determine the design level and the associated limits after the average wind velocity of the erection site has been established.

## APPENDIX

### Methodology for Calculating the Economy of Generation Plants Driven by Wind (kWh - Net Costs)

The net cost of a kilowatt hour produced by a wind generation station can be calculated according to the formula

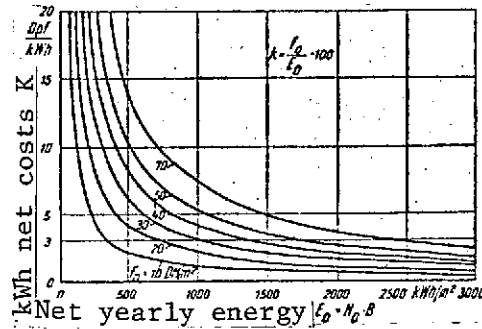


Figure 9. Dependence of the kWh net costs on the produced net yearly energy  $E_0$  for various specific yearly costs  $f_0$ .

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$$k = \frac{100 \cdot f_0}{N_0 \cdot B} + c \text{ (Dpf/kWh)}$$

Here we have  $f_0 = z \cdot K_{a0}$ , the fixed specific yearly costs of the installed power (in DM/m<sup>2</sup>), if  $z$  is the yearly cost factor and  $K_{a0}$  is the specific installation costs,  $N_0$  the installed specific generator power (in kW/m<sup>2</sup>),  $B = E_0/N_0$  the operation period (in hours) where  $E_0$  = specific net yearly energy (in kWh/m<sup>2</sup>) and  $c$  is the performance-dependent costs (in Dpf/kWh) (for wind generation plants practically equal to zero).

Figure 9 gives the quantity  $k$  in the function of the denominator of the formula given above, and  $f_0$  is the parameter (family of hyperbolas). The denominator  $N_0 \cdot B = E_0$  (kWh/m<sup>2</sup> years) is the specific yearly net power of a wind generation station assuming that the energy produced by the wind supply is completely exploited in the form of work and delivered to the connected network. Using the variables discussed above, we find the following optimum

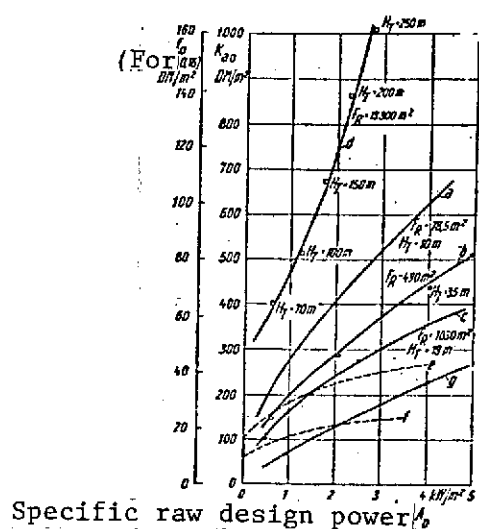


Figure 10. Dependence of specific construction costs  $K_{ao}$  and fixed yearly costs  $f_o$  for various installations on the specific net design power  $A_o$

net values for a wind-controlled installation:\* This defines all

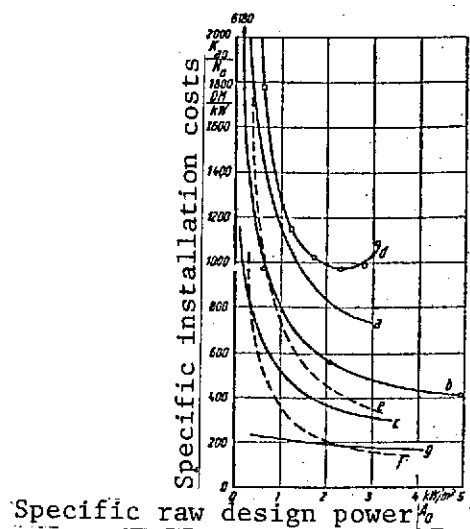
$$E_o = \Sigma W_o \cdot \Sigma P_{max} \cdot \eta c_1 \quad \text{and} \quad N_o = A_o \cdot \eta c_1$$

variables. Figure 9 shows an example. In order to obtain a net  $k = 3 \text{ DM/kWh}$  for a yearly cost contribution of  $f_o = 20 \text{ DM/m}^2$ , the net yearly energy  $E_o$  of the erection site must be at least  $700 \text{ kWh/m}^2$ . If it is assumed that  $\Sigma P_{max} = 0.5$  and  $\eta c_1 = 0.3$  and that these are possible, then the wind location must have a raw yearly energy level of at least

$$\Sigma W_o = \frac{E_o}{\Sigma P_{max} \eta c_1} = \frac{700}{0.50 \cdot 0.3} = 4700 \text{ kWh/m}^2$$

According to Figure 7, this corresponds to  $v_m = 7.5 \text{ m/s}$  ( $\pm 1$ ) percent, (North Sea Coast). For the case that  $f_o$  can be reduced to 10,

\* For a net-controlled installation,  $E_o$  must be multiplied by the reduction factor  $\eta_R = 0.8$  to 0.9.



a- 10-m Allgaier installation ( $F_R = 78,5 \text{ m}^2$ ,  $\eta_{c1} = 0,245$ ), b- 25-m installation, dissertation U. Hutter, page 25 ( $F_R = 450 \text{ m}^2$ ,  $\eta_{c1} = 0,234$ ), c- 100-kW project of the study association wind generation ( $F_R = 1030 \text{ m}^2$ ,  $\eta_{c1} = 0,310$ ). d- Kleinhenz project ( $F_R = 13\,300 \text{ m}^2$ ,  $\eta_{c1} = 0,301$ ), e-f- theoretical costs for series production, 10-m Allgaier installation (e) and 100 kW project of the study association, (f), g- most economical installation according to Figure 9 ( $F_R = 2000 \text{ m}^2$ ,  $\eta_{c1} = 0,35$ ). In installations b and d we have set 1 RM = 2 DM. HT tower height. In Figure 11: a to g, see caption for Figure 10.

Figure 11. Specific construction costs of various installations per unit of power as a function of specific raw design power  $A_o$ .

DM/m<sup>2</sup>, the values would be:

$$E_o = 350 \text{ kWh/m}^2 \text{ and } v_w = \frac{350}{0,15} = 2340 \text{ kWh/m}^2.$$

i.e.,  $v_m = 5.8 \text{ m/sec}$  (North German Flatland).

The specific installation costs  $K_{ao}$  or the specific yearly costs  $f_o$  for  $z = 0.16$  are shown in Figure 10 as a function of  $A_o$  for a few installations. The power level dependence of  $K_{ao}$  was calculated assuming that the costs are increased by 50% when the design power level  $A_o$  is doubled. For clarity, we also show the dependence of the installation costs in DM/kW referred to the

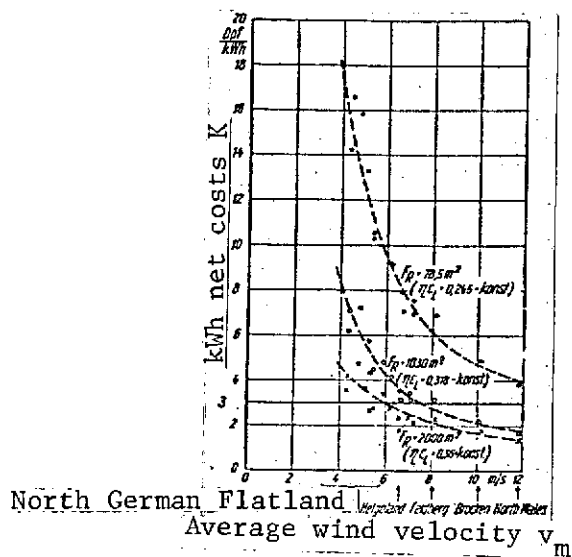


Figure 12. kWh net costs  $K$  is a function of average wind velocity  $v_m$ .

installed power level  $K_{a0}/N_0$ , which is usually done in the electrical power plant literature.

Figure 12 shows the net costs per kWh for the three different installations and for the 14 measurements installations given in the top of Table 2. The dashed curves were calculated using the formulas given above.

This representation concludes the methodology of the calculation. The absolute numbers for  $k$  are not intended to be correct, because the installation costs,  $K_{a0}$  and their dependence on  $A_0$  were partly estimated.



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